

# Ontologies - Querying Data through Ontologies

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# Outline

- 1 Introduction
  - The Semantic Web
  - Ontologies and Reasoning
  - Illustration
- 2 3 ontology languages for the Web
- 3 Reasoning in Description Logics
- 4 Querying Data through Ontologies
- 5 Conclusion

# The Semantic Web

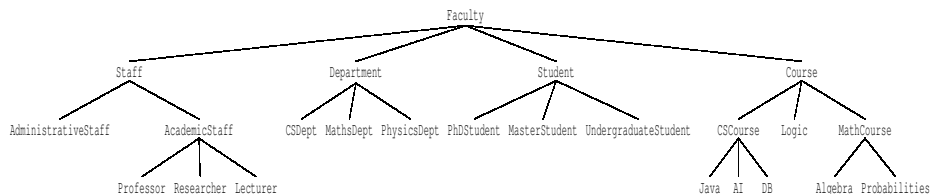
- A Web in which the resources are **semantically** described
  - ▶ annotations give information about a page, explain an expression in a page, etc.
- More precisely, a resource is anything that can be referred to by a **URI**
  - ▶ a web page, identified by a URL
  - ▶ a fragment of an XML document, identified by an element node of the document,
  - ▶ a web service,
  - ▶ a thing, an object, a concept, a property, etc.
- Semantic annotations: logical assertions that relate resources to some terms in pre-defined **ontologies**

# Ontologies

- Formal descriptions providing **human** users a shared understanding of a given domain
  - ▶ A controlled vocabulary
- Formally defined so that it can also be processed by **machines**
- **Logical semantics** that enables **reasoning**.
- Reasoning is the key for different important tasks of Web data management, in particular
  - ▶ to answer queries (over possibly distributed data)
  - ▶ to relate objects in different data sources enabling their integration
  - ▶ to detect inconsistencies or redundancies
  - ▶ to refine queries with too many answers, or to relax queries with no answer

# Classes and class hierarchy

- Backbone of the ontology
- AcademicStaff is a **Class**
- (A class will be interpreted as a **set** of objects)
- AcademicStaff **isa** Staff
- (isa is interpreted as set inclusion)



# Relations

- Declaration of **relations** with their **signature**
- (Relations will be interpreted as binary relations between objects)
- `TeachesIn(AcademicStaff, Course)`
  - ▶ if one states that “`X TeachesIn Y`”, then `X` belongs to `AcademicStaff` and `Y` to `Course`,
- `TeachesTo(AcademicStaff, Student)`,
- `Leads(Staff, Department)`

# Instances

- Classes have **instances**
- Dupond is an instance of the class Professor
- it corresponds to the fact: Professor(Dupond)
  
- Relations also have **instances**
- (Dupond,CS101) is an instance of the relation TeachesIn
- it corresponds to the fact: TeachesIn(Dupond,CS101)
  
- The instance statements can be seen as (and stored in) a **database**

# Ontology = schema + instance

- **Schema**

- ▶ The set of class and relation names
- ▶ The **signatures** of relations and also **constraints**
- ▶ The constraints that are used for two purposes
  - ★ checking data consistency (like dependencies in databases)
  - ★ inferring new facts

- **Instance**

- ▶ The set of facts
- ▶ The set of base facts together with the inferred facts should satisfy the constraints

- **Ontology** (i.e., **Knowledge Base**) = Schema + Instance



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## 3 ontology languages for the Web

- RDF: a very simple ontology language
  - RDFS: Schema for RDF
    - ▶ Can be used to define richer ontologies
  - OWL: a much richer ontology language
- 
- We next present them rapidly
  - We will introduce further a family of ontology languages: Description logics

# RDF: Resource Description Framework

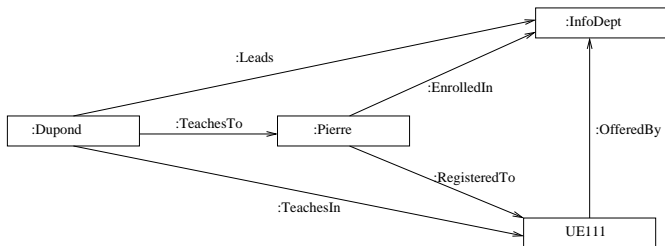
- RDF facts are triplets

```
< :Dupond :Leads :CSDept >  
< :Dupond :TeachesIn :UE111 >  
< :Dupond :TeachesTo :Pierre >  
< :Pierre :EnrolledIn :CSDept >  
< :Pierre :RegisteredTo :UE111 >  
< :UE111 :OfferedBy :CSDept >
```

- Linked open data: publish open data sets on the Web
  - ▶ By September 2011, 31 billions RDF triplets

# RDF graph

- A set of RDF facts defines
  - ▶ a set of relations between objects
  - ▶ an **RDF graph** where the nodes are objects:



# RDF semantics

- A triplet  $\langle s \ P \ o \rangle$  is interpreted in first-order logic (FOL) as a fact  $P(s, o)$
- Example:

```
Leads(Dupond, CSDept)
TeachesIn(Dupond, UE111)
TeachesTo(Dupond, Pierre)
EnrolledIn(Pierre, CSDept)
RegisteredTo(Pierre, UE111)
OfferedBy(UE111, CSDept)
```

## RDFS: RDF Schema

- Not detailed here: the schema in RDF is super simplistic
- An **RDF Schema** defines the schema of a richer ontology

# RDF Schema

- Do not get confused: RDFS can use RDF as syntax, i.e., RDFS statements can be themselves expressed as RDF triplets using some specific **properties** and **objects** used as RDFS keywords with a particular meaning.
- Declaration of classes and subclass relationships
  - ▶ `< Staff rdf:type rdfs:Class >`
  - ▶ `< Java rdfs:subClassOf CSCourse >`
- Declaration of instances (beyond the pure schema)
  - ▶ `< Dupond rdf:type AcademicStaff >`

## RDF Schema - continued

- Declaration of relations (properties in RDFS terminology)
  - ▶ `< RegisteredTo rdf:type rdf:Property >`
- Declaration of subproperty relationships
  - ▶ `< LateRegisteredTo rdfs:subPropertyOf RegisteredTo >`
- Declaration of domain and range restrictions for predicates
  - ▶ `< TeachesIn rdfs:domain AcademicStaff >`
  - ▶ `< TeachesIn rdfs:range Course >`
  - ▶ `TeachesIn(AcademicStaff, Course)`



## RDFS logical semantics

RDF and RDFS statements	FOL translation	DL notation
$\langle i \text{ rdf:type } C \rangle$	$C(i)$	$i : C$ or $C(i)$
$\langle i P j \rangle$	$P(i, j)$	$i P j$ or $P(i, j)$
$\langle C \text{ rdfs:subClassOf } D \rangle$	$\forall X (C(X) \Rightarrow D(X))$	$C \sqsubseteq D$
$\langle P \text{ rdfs:subPropertyOf } R \rangle$	$\forall X \forall Y (P(X, Y) \Rightarrow R(X, Y))$	$P \sqsubseteq R$
$\langle P \text{ rdfs:domain } C \rangle$	$\forall X \forall Y (P(X, Y) \Rightarrow C(X))$	$\exists P \sqsubseteq C$
$\langle P \text{ rdfs:range } D \rangle$	$\forall X \forall Y (P(X, Y) \Rightarrow D(Y))$	$\exists P^- \sqsubseteq D$

- Ignore for now DL column
- This is just a notation
- We will come back to it to discuss Description logics

# OWL: Web Ontology Language

- OWL extends RDFS with the possibility to express additional constraints
- Main OWL constructs
  - ▶ Disjointness between classes
  - ▶ Constraints of functionality and symmetry on predicates
  - ▶ Intentional class definitions
  - ▶ Class union and intersection
- We will see these are all expressible in Description logics

## OWL constructs

- Ignore again the DL column
- Disjointness between classes:

OWL notation	FOL translation	DL notation
$\langle C \text{ owl:disjointWith } D \rangle$	$\forall X (C(X) \Rightarrow \neg D(X))$	$C \sqsubseteq \neg D$

- Constraints of functionality and symmetry on predicates:

OWL notation	FOL translation	DL notation
$\langle P \text{ rdf:type owl:FunctionalProperty} \rangle$	$\forall X \forall Y \forall Z (P(X, Y) \wedge P(X, Z) \Rightarrow Y = Z)$	$(\text{func } P)$ or $\exists P \sqsubseteq (\leq 1 P)$
$\langle P \text{ rdf:type owl:InverseFunctionalProperty} \rangle$	$\forall X \forall Y \forall Z (P(X, Y) \wedge P(Z, Y) \Rightarrow X = Z)$	$(\text{func } P^-)$ or $\exists P^- \sqsubseteq (\leq 1 P^-)$
$\langle P \text{ owl:inverseOf } Q \rangle$	$\forall X \forall Y (P(X, Y) \Leftrightarrow Q(Y, X))$	$P \equiv Q^-$
$\langle P \text{ rdf:type owl:SymmetricProperty} \rangle$	$\forall X \forall Y (P(X, Y) \Rightarrow P(Y, X))$	$P \sqsubseteq P^-$

## Definition of intentional classes in OWL

- Goal: allow expressing complex constraints such as:
  - ▶ departments can be lead only by professors
  - ▶ only professors or lecturers may teach to undergraduate students.
- The keyword `owl:Restriction` is used in association with a **blank node class**, and some specific restriction properties:
  - ▶ `owl:someValuesFrom`
  - ▶ `owl:allValuesFrom`
  - ▶ `owl:minCardinality`
  - ▶ `owl:maxCardinality`

# OWL Semantics

OWL notation	FOL translation	DL notation
<code>_a owl:onProperty P</code> <code>_a owl:allValuesFrom C</code>	$\forall Y (P(X, Y) \Rightarrow C(Y))$	$\forall P.C$
<code>_a owl:onProperty P</code> <code>_a owl:someValuesFrom C</code>	$\exists Y (P(X, Y) \wedge C(Y))$	$\exists P.C$
<code>_a owl:onProperty P</code> <code>_a owl:minCardinality n</code>	$\exists Y_1 \dots \exists Y_n (P(X, Y_1) \wedge \dots \wedge P(X, Y_n) \wedge \bigwedge_{i,j \in [1..n], i \neq j} (Y_i \neq Y_j))$	$(\geq nP)$
<code>_a owl:maxCardinality n</code>	$\forall Y_1 \dots \forall Y_n \forall Y_{n+1} (P(X, Y_1) \wedge \dots \wedge P(X, Y_n) \wedge P(X, Y_{n+1}) \Rightarrow \bigvee_{i,j \in [1..n+1], i \neq j} (Y_i = Y_j))$	$(\leq nP)$

## Unnamed new classes by example

- Departments can be lead only by professors

- Define the set of objects that are lead by professors

```
_a rdfs:subClassOf owl:Restriction
_a owl:onProperty Leads
_a owl:allValuesFrom Professor
```

- Now specify that all departments are lead by professors

```
Department rdfs:subClassOf _a
```

## Union and Intersection of Classes by example

- only professors or lecturers may teach to undergraduate students

```

_a rdfs:subClassOf owl:Restriction
_a owl:onProperty TeachesTo
_a owl:someValuesFrom Undergrad
_b owl:unionOf (Professor, Lecturer)
_a rdfs:subClassOf _b

```

- This corresponds to an inclusion axiom in Description Logic:

$$\exists \textit{TeachesTo}.\textit{UndergraduateStudent} \sqsubseteq \textit{Professor} \sqcup \textit{Lecturer}$$

- `owl:equivalentClass` corresponds to double inclusion:

$$\textit{MathStudent} \equiv \textit{Student} \sqcap \exists \textit{RegisteredTo}.\textit{MathCourse}$$

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  - $\mathcal{ALC}$
  - Polynomial DLs
- 4 Querying Data through Ontologies
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# Description Logics

- Philosophy: isolate **decidable** fragments of first-order logic allowing reasoning on complex logical axioms over unary and binary predicates
- These fragments are called **Description Logics**
  
- The DL jargon:
  - ▶ the classes are called **concepts**
  - ▶ the properties are called **roles**.
  - ▶ the ontology (the **knowledge base**) = Tbox + Abox
  - ▶ the schema is called the **Tbox**
  - ▶ the instance is called the **Abox**

# The DL family

- Few constructs: atomic concepts and roles, inverse of roles, unqualified restriction on roles, restricted negation
- Revisit RDFS checking out the DL column
- If you don't like the syntax: **neither do I**

# Semantics of main constructs

- $I(C_1 \sqcap C_2) = I(C_1) \cap I(C_2)$
- $I(\forall R.C) = \{o_1 \mid \forall o_2 [(o_1, o_2) \in I(R) \Rightarrow o_2 \in I(C)]\}$
- $I(\exists R.C) = \{o_1 \mid \exists o_2. [(o_1, o_2) \in I(R) \wedge o_2 \in I(C)]\}$
- $I(\neg C) = \Delta^I \setminus I(C)$
- $I(R^-) = \{(o_2, o_1) \mid (o_1, o_2) \in I(R)\}$

## Defining a particular description logic

- Define how to construct complex concepts and roles starting from atomic concepts and roles
  - ▶ *Professor*  $\sqcup$  *Lecturer* (those who are either professor or lecturer)
- Choose the constraints you want to consider
- The **complexity** of the logic depends on these choices

## Reasoning problems studied in DL

- **Satisfiability checking:** Given a DL knowledge base  $\mathcal{K} = \langle \mathcal{T}, \mathcal{A} \rangle$ , is  $\mathcal{K}$  satisfiable?
- **Subsumption checking:** Given a Tbox  $\mathcal{T}$  and two concept expressions  $C$  and  $D$ , does  $\mathcal{T} \models C \sqsubseteq D$ ?
- **Instance checking:** Given a DL knowledge base  $\mathcal{K} = \langle \mathcal{T}, \mathcal{A} \rangle$ , an individual  $e$  and a concept expression  $C$ , does  $\mathcal{K} \models C(e)$ ?
- **Query answering:** Given a DL knowledge base  $\mathcal{K} = \langle \mathcal{T}, \mathcal{A} \rangle$ , and a concept expression  $C$ , finds the set of individuals  $e$  such that  $\mathcal{K} \models C(e)$ ?

## Remarks

- For DLs with full negation: instance checking and subsumption checking can be reduced to (un)satisfiability checking
  - ▶  $\mathcal{T} \models C \sqsubseteq D \Leftrightarrow \langle \mathcal{T}, \{(C \sqcap \neg D)(a)\} \rangle$  is unsatisfiable.
  - ▶  $\langle \mathcal{T}, \mathcal{A} \rangle \models C(e) \Leftrightarrow \langle \mathcal{T}, \mathcal{A} \cup \{\neg C(e)\} \rangle$  is unsatisfiable.
- For DLs without negation: instance checking can be reduced to subsumption checking by computing the **most specific concept** satisfied by an individual in the Abox (denoted  $msc(\mathcal{A}, e)$ )
  - ▶  $\langle \mathcal{T}, \mathcal{A} \rangle \models C(e) \Leftrightarrow \mathcal{T} \models msc(\mathcal{A}, e) \sqsubseteq C$

# ALC: the prototypical DL

- (standard) An ALC Abox is made of a set of facts of the form  $C(a)$  and  $R(a, b)$  where  $a$  and  $b$  are individuals,  $R$  is an atomic role and  $C$  is a possibly complex concept
- ALC constructs:
  - ▶ **conjunction**  $C_1 \sqcap C_2$ ,
  - ▶ **existential restriction**  $\exists R.C$ 
    - ★  $\exists Y(R(X, Y) \wedge C(Y))$
  - ▶ **negation**  $\neg C$ .
- As a result, ALC also contains de facto:
  - ▶ **disjunctions**  $C_1 \sqcup C_2 (\equiv \neg(\neg C_1 \sqcap \neg C_2))$ ,
  - ▶ **value restrictions**  $(\forall R.C \equiv \neg(\exists R.\neg C))$ ,
  - ▶  $\top (\equiv A \sqcup \neg A)$  and  $\perp (\equiv A \sqcap \neg A)$ .

## ALC - continued

- An ALC Tbox may contain inclusion constraints between concepts and roles

$$\begin{aligned} \textit{MathCourse} &\sqsubseteq \textit{Course} \\ \textit{LateRegisteredTo} &\sqsubseteq \textit{RegisteredTo} \end{aligned}$$

- An ALC Tbox may contain **General Concept Inclusions** (GCIs):  
 $\exists \textit{TeachesTo}.\textit{UndergraduateStudent} \sqsubseteq \textit{Professor} \sqcup \textit{Lecturer}$



## Tableau method

- Reasoning is based on tableau calculus - a classical method in logic for checking satisfiability
- Extensively used in Description logics for implementing reasoners
- Technique
  - ▶ Get rid of the Tbox by recursively unfolding the concept definitions
  - ▶ Transform the resulting Abox so that negations applies only to atomic concepts
  - ▶ Try to construct a model or raise a contradiction
- We illustrate the technique with a simple example without GCIs
- In general, much more involved

## Tableau method

- For satisfiability checking of a DL knowledge base  $\langle \mathcal{T}, \mathcal{A} \rangle$ 
  - ▶  $\mathcal{T} = \{C_1 \equiv A \sqcap B, C_2 \equiv \exists R.A, C_3 \equiv \forall R.B, C_4 \equiv \forall R. \neg C_1\}$
  - ▶  $\mathcal{A} = \{C_2(a), C_3(a), C_4(a)\}$
- Get rid of the Tbox, by recursively **unfolding** the concept definitions:
  - ▶  $\mathcal{A}' = \{(\exists R.A)(a), (\forall R.B)(a), (\forall R. \neg(A \sqcap B))(a)\} \equiv \langle \mathcal{T}, \mathcal{A} \rangle$
- Transform the concepts expressions in  $\mathcal{A}'$  into **negation normal form**
  - ▶  $\mathcal{A}'' = \{(\exists R.A)(a), (\forall R.B)(a), (\forall R. (\neg A \sqcup \neg B))(a)\}$
- Apply **tableau rules** to **extend** the resulting Abox until no rule applies anymore:
  - ▶ From an extended Abox which is **complete** (no rule applies) and **clash-free** (no obvious contradiction), a so-called **canonical interpretation** can be built, which is a model of the initial Abox.

## Tableau rules for $\mathcal{ALC}$

- The  $\sqcap$ -rule:

**Condition:**  $\mathcal{A}$  contains  $(C \sqcap D)(a)$  but not both  $C(a)$  and  $D(a)$

**Action:** add  $\mathcal{A}' = \mathcal{A} \cup \{C(a), D(a)\}$

- The  $\sqcup$ -rule:

**Condition:**  $\mathcal{A}$  contains  $(C \sqcup D)(a)$  but neither  $C(a)$  nor  $D(a)$

**Action:** add  $\mathcal{A}' = \mathcal{A} \cup \{C(a)\}$  and  $\mathcal{A}'' = \mathcal{A} \cup \{D(a)\}$

- The  $\exists$ -rule:

**Condition:**  $\mathcal{A}$  contains  $(\exists R.C)(a)$  but there is no  $c$  such that  $\{R(a, c), C(c)\} \subseteq \mathcal{A}$

**Action:** add  $\mathcal{A}' = \mathcal{A} \cup \{R(a, b), C(b)\}$  where  $b$  is a new individual name

- The  $\forall$ -rule:

**Condition:**  $\mathcal{A}$  contains  $(\forall R.C)(a)$  and  $R(a, b)$  but not  $C(b)$

**Action:** add  $\mathcal{A}' = \mathcal{A} \cup \{C(b)\}$

## Illustration on the example

- The result of the application of the tableau method to  $\mathcal{A}'' = \{(\exists R.A)(a), (\forall R.B)(a), (\forall R.(\neg A \sqcup \neg B))(a)\}$  gives the following Aboxes:
  - ▶  $\mathcal{A}_1'' = \mathcal{A}'' \cup \{R(a,b), A(b), B(b), \neg A(b)\}$
  - ▶  $\mathcal{A}_2'' = \mathcal{A}'' \cup \{R(a,b), A(b), B(b), \neg B(b)\}$
- They both contain a **clash**:  
 $\mathcal{A}''$  (and the equivalent original knowledge base) is **correctly decided unsatisfiable** by the algorithm

## Complexity

- The tableau method shows that the satisfiability of  $\mathcal{ALC}$  knowledge bases is decidable but with a complexity that may be **exponential** because of the disjunction construct and the associated  $\sqcup$ -rule.
- Satisfiability checking in  $\mathcal{ALC}$  (and thus also subsumption and instance checking) is in fact **EXPTIME-complete**
- Additional constructs like those in the fragment **OWL DL** of OWL do not change the complexity class of reasoning (which remains EXPTIME-complete)
- **OWL Full** is undecidable

# DLs for which reasoning is polynomial

- $\mathcal{FL}$ : conjunction  $C_1 \sqcap C_2$ , value restrictions  $\forall R.C$  and unqualified existential restriction  $\exists R$ 
  - ▶ For Tboxes without GCIs, subsumption checking is polynomial
  - ▶ For Tboxes with (even simple) GCIs, subsumption checking is co-NP complete
- $\mathcal{EL}$ : conjunctions  $C_1 \sqcap C_2$  and existential restrictions  $\exists R.C$ 
  - ▶ Subsumption checking in  $\mathcal{EL}$  is polynomial even for general Tboxes.
- $\mathcal{FL\mathcal{E}}$ : conjunction  $C_1 \sqcap C_2$ , value restrictions  $\forall R.C$ , and existential restrictions  $\exists R.C$ 
  - ▶ Subsumption checking in  $\mathcal{FL\mathcal{E}}$  is NP-complete
- The DL-LITE family: a good trade-off, specially designed for guaranteeing query answering through ontologies to be polynomial in data complexity.

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  - Querying using RDFS
  - Querying using DL-LITE
  - Complexity
- 5 Conclusion

# Querying using RDFS

- RDFS statements can be used to infer new triples
- Example
  - ▶ Base fact  $ResponsibleOf(durand, ue111)$
  - ▶ Use the statement  $\langle ResponsibleOf \text{ rdfs:domain } Professor \rangle$   
i.e., the logical rule:  $ResponsibleOf(X, Y) \Rightarrow Professor(X)$
  - ▶ With substitution  $\{X/durand, Y/ue111\}$
  - ▶ Infer fact  $Professor(durand)$
  - ▶ Use the statement  $\langle Professor \text{ rdfs:subClassOf } AcademicStaff \rangle$   
i.e., the rule  $Professor(X) \Rightarrow AcademicStaff(X)$
  - ▶ With substitution  $\{X/durand\}$
  - ▶ Infer fact  $AcademicStaff(durand)$
  - ▶ etc.



# The saturation algorithm

- Keep inferring new facts until a fixpoint is reached
- Note: Only polynomially many facts can be added
- PTIME

## Querying using DL-LITE

- Develop as a good compromise between expressive power and reasonable complexity of query answering
- RDFS simpler and very used but limited
- More complex DL: query answering is unfeasible

# The DL-LITE family

- Three kinds of axioms: **positive inclusions** (PI), **negative inclusions** (NI) and **functionality** constraints (func)
- Captures the main constraints used in Databases and Software Engineering
- Different variants
  - ▶ DL-LITE $\mathcal{R}$ : no functionality constraints
  - ▶ DL-LITE $\mathcal{F}$ : no role inclusion
  - ▶ DL-LITE $\mathcal{A}$ : no functionality constraints on roles involved in role inclusions

## PI: Positive inclusion and incompleteness

- One of the following forms:

DL notation	Corresponding logical rule
$B \sqsubseteq \exists P$	$B(X) \Rightarrow \exists Y P(X, Y)$
$\exists Q \sqsubseteq \exists P$	$Q(X, Y) \Rightarrow \exists Z P(X, Z)$
$B \sqsubseteq \exists P^-$	$B(X) \Rightarrow \exists Y P(Y, X)$
$\exists Q \sqsubseteq \exists P^-$	$Q(X, Y) \Rightarrow \exists Z P(Z, X)$
$P \sqsubseteq Q^-$ or $P^- \sqsubseteq Q$	$P(X, Y) \Rightarrow Q(Y, X)$

where  $P$  and  $Q$  denote properties and  $B$  denotes a class.

DL notation	Corresponding logical rule
$Professor \sqsubseteq \exists TeachesIn$	$Professor(X) \Rightarrow \exists Y TeachesIn(X, Y)$
$Course \sqsubseteq \exists RegisteredIn^-$	$Course(X) \Rightarrow \exists Y RegisteredIn(Y, X)$

- Not **safe**
- From  $Professor(durand)$ , I know there is some  $y$   $TeachesIn(durand, y)$
- Incompleteness: I don't know  $y$
- Saturation may not terminate

## Negative inclusion and inconsistencies

- Negative inclusion takes one of the forms:

$$\begin{array}{c} \text{DL notation} \\ \hline B_1 \sqsubseteq \neg B_2 \\ \hline R_1 \sqsubseteq \neg R_2 \\ \hline \end{array}$$

- where  $B_1$  and  $B_2$  are either classes or expressions of the form  $\exists P$  or  $\exists P^-$  for some property  $P$
  - and where  $R_1$  and  $R_2$  are either properties or inverses of properties.
- Students do not teach courses

DL notation	Corresponding logical rule
$Student \sqsubseteq \neg \exists TeachesIn$	$Student(X) \Rightarrow \neg \exists Y TeachesIn(X, Y)$ or equivalently, $\exists Y TeachesIn(X, Y) \Rightarrow \neg Student(X)$

- The knowledge base may be **inconsistent**
- Not possible with RDFS ontologies

## Key constraints and more inconsistencies.

- Axioms of the form  $(\text{funct } P)$  or  $(\text{funct } P^-)$  where  $P$  is a property

DL notation	corresponding logical rule
$(\text{funct } P)$	$P(X, Y) \wedge P(X, Z) \Rightarrow Y = Z$
$(\text{funct } P^-)$	$P(Y, X) \wedge P(Z, X) \Rightarrow Y = Z$

- Key constraints also lead to inconsistencies
- Example:
  - ▶  $(\text{funct } \text{ResponsibleOf}^-)$
  - ▶ A course must have a unique professor responsible for it
  - ▶ If we have  $\text{ResponsibleOf}(\text{durand}, \text{ue111})$  and  $\text{ResponsibleOf}(\text{dupond}, \text{ue111})$   
The KB is inconsistent

# Query answering: Example

- Abox:
  - ▶  $Professor(Jim), HasTutor(John, Mary), TeachesTo(John, Bill)$
- Tbox:
  - ▶  $Professor \sqsubseteq \exists TeachesTo$
  - ▶  $Student \sqsubseteq \exists HasTutor$
  - ▶  $\exists TeachesTo^- \sqsubseteq Student$
  - ▶  $\exists HasTutor^- \sqsubseteq Professor$
  - ▶  $Professor \sqsubseteq \neg Student$
- Queries: conjunctive queries on concepts and atomic roles
  - ▶  $q_0(x) \leftarrow TeachesTo(x, y) \wedge HasTutor(y, z)$

## Query answering: Principles of reformulation

- Transform the query into FO queries over the database
- FO queries are used to check for inconsistencies of the KB
- FO queries are used to evaluate the result
- The FO queries can be evaluated using a database engine with query optimization
- Because of incompleteness, not always possible



# Query answering by example (no inconsistency)

- Tbox:  $\mathcal{T}$ 
  - ▶  $Professor \sqsubseteq \exists TeachesTo$
  - ▶  $Student \sqsubseteq \exists HasTutor$
  - ▶  $\exists TeachesTo^- \sqsubseteq Student$
  - ▶  $\exists HasTutor^- \sqsubseteq Professor$
  - ▶  $Professor \sqsubseteq \neg Student$
- Query:
  - ▶  $q_0(x) \leftarrow TeachesTo(x, y) \wedge HasTutor(y, z)$
- Reformulations of  $q_0$  given the the Tbox  $\mathcal{T}$ :
  - ▶  $q_1(x) \leftarrow TeachesTo(x, y) \wedge Student(y)$
  - ▶  $q_2(x) \leftarrow TeachesTo(x, y) \wedge TeachesTo(z', y)$
  - ▶  $q_3(x) \leftarrow TeachesTo(x, y')$
  - ▶  $q_4(x) \leftarrow Professor(x)$
  - ▶  $q_5(x) \leftarrow HasTutor(u, x)$
- **Main result (holds for DL-LITE<sub>A</sub> but not for full DL-LITE):**
  - ▶ For any Abox  $\mathcal{A}$  such that  $\mathcal{T} \cup \mathcal{A}$  is satisfiable:  
 $Answer(q_0, \mathcal{T} \cup \mathcal{A}) = \bigcup_i Answer(q_i, \mathcal{A})$

# Illustration

- $q_0(x) \leftarrow \textit{TeachesTo}(x, y) \wedge \textit{HasTutor}(y, z)$
- $\textit{Student} \sqsubseteq \exists \textit{HasTutor}$
- $\textit{HasTutor}(y, z) \leftarrow \textit{Student}(y)$
- $q_1(x) \leftarrow \textit{TeachesTo}(x, y) \wedge \textit{Student}(y)$

## Example (ctd)

- Abox:  $\mathcal{A}$ 
  - ▶  $Professor(Jim), HasTutor(John, Mary), TeachesTo(John, Bill)$
- Query
  - ▶  $q_0(x) \leftarrow TeachesTo(x, y) \wedge HasTutor(y, z)$
- Reformulations of  $q_0$  given the the Tbox  $\mathcal{T}$ :
  - ▶  $q_1(x) \leftarrow TeachesTo(x, y) \wedge Student(y)$
  - ▶  $q_2(x) \leftarrow TeachesTo(x, y) \wedge TeachesTo(z', y)$
  - ▶  $q_3(x) \leftarrow TeachesTo(x, y')$
  - ▶  $q_4(x) \leftarrow Professor(x)$
  - ▶  $q_5(x) \leftarrow HasTutor(u, x)$
- Result of the evaluation of the reformulations over  $\mathcal{A}$ :
  - ▶  $Answer(q_0, \mathcal{T} \cup \mathcal{A}) = \{Mary, Jim, John\}$

# Consistency checking by example

- Tbox:  $\mathcal{T}'$ 
  - ▶  $Professor \sqsubseteq \exists TeachesTo$
  - ▶  $Student \sqsubseteq \exists HasTutor$
  - ▶  $\exists TeachesTo^- \sqsubseteq Student$
  - ▶  $\exists HasTutor^- \sqsubseteq Professor$
  - ▶  $Professor \sqsubseteq \neg Student$
  - ▶  $\exists TeachesTo \sqsubseteq \neg Student$
  - ▶  $\exists HasTutor \sqsubseteq Student$
- Saturation of the NIs (possibly using the PIs):
  - ▶  $\exists TeachesTo \sqsubseteq \neg \exists HasTutor$
- Translation of each NI into a boolean conjunctive query:
  - ▶  $q_{unsat} \leftarrow TeachesTo(x, y) \wedge HasTutor(x, y')$
- Evaluation of  $q_{unsat}$  on the Abox  $\mathcal{A}$ :
  - ▶  $\{Professor(Jim), HasTutor(John, Mary), TeachesTo(John, Bill)\}$
  - ▶  $Answer(q_{unsat}, \mathcal{A}) = true$
- **Main result:**
  - ▶  $\mathcal{T}' \cup \mathcal{A}$  is inconsistent iff there exists a  $q_{unsat}$  such that  $Answer(q_{unsat}, \mathcal{A}) = true$

- Closure of a Tbox: derive new statements
- From  $\exists \textit{TeachesTo} \sqsubseteq \neg \textit{Student}$
- Derive  $\textit{Student} \sqsubseteq \neg \exists \textit{TeachesTo}$
- From  $\exists \textit{HasTutor} \sqsubseteq \textit{Student}$  and  $\textit{Student} \sqsubseteq \neg \exists \textit{TeachesTo}$
- Derive  $\exists \textit{HasTutor} \sqsubseteq \neg \exists \textit{TeachesTo}$
- From  $\exists \textit{HasTutor} \sqsubseteq \neg \exists \textit{TeachesTo}$
- Derive  $\exists \textit{TeachesTo} \sqsubseteq \neg \exists \textit{HasTutor}$

# FOL reducibility of data management in DL-LITE

Query answering and data consistency checking can be performed in two separate steps:

- 1 A reasoning step with the Tbox alone (i.e., the ontology without the data) and some conjunctive queries
- 2 An evaluation step of conjunctive queries over the data in the Abox (without the Tbox)
  - ▶ makes it possible to use an SQL engine
  - ▶ thus taking advantage of well-established query optimization strategies supported by standard relational DBMS

## Complexity results

- The **reasoning step** on Tbox is **polynomial** in the size of the Tbox
  - ▶ Produces a polynomial number of reformulations and of *unsat* queries
- The **evaluation step** over the Abox has the **same data complexity as standard evaluation of conjunctive queries over relational databases**
  - ▶ in  $AC_0$  (strictly contained in *LogSpace* and thus in  $P$ )
- The interaction between role inclusion constraints and functionality constraints makes reasoning in DL-LITE  **$P$ -complete in data complexity**
  - ▶ full DL-LITE is **not FOL-reducible**
  - ▶ Reformulating a query may require recursion

## Problem with full DL-LITE by example

- Let the Tbox ( $R$  and  $P$  are two properties and  $S$  is a class):

$$R \sqsubseteq P$$

$$(\text{funct } P)$$

$$S \sqsubseteq \exists R$$

$$\exists R^{-} \sqsubseteq \exists R$$

- and the query:  $q(x) :- R(z, x)$
- $r_1(x) :- S(x_1), P(x_1, x)$  is a reformulation of the query  $q$  given the Tbox
  - from  $S(x_1)$  and the PI  $S \sqsubseteq \exists R$ , it can be inferred:  $\exists y R(x_1, y)$ , and thus  $\exists y P(x_1, y)$  (since  $R \sqsubseteq P$ ).
  - from the functionality constraint on  $P$  and  $P(x_1, x)$ , it can be inferred:  $y = x$ , and thus:  $R(x_1, x)$
  - Therefore:  $\exists x_1 S(x_1) \wedge P(x_1, x) \models \exists z R(z, x)$  (i.e.,  $r_1(x)$  is contained in the query  $q(x)$ )



## Problem with full DL-LITE by example - continued

- $r_1$  is not the only one reformulation of the query
- In fact, there exists an *infinite* number of different reformulations for  $q(x)$ :
- for  $k \geq 2$ ,  $r_k(x) :- S(x_k), P(x_k, x_{k-1}), \dots, P(x_1, x)$  is also a reformulation:
  - ▶ from  $S(x_k)$  and the PI  $S \sqsubseteq \exists R$ , it can be inferred:  $\exists y_k R(x_k, y_k)$ , and thus  $\exists y_k P(x_k, y_k)$  (since  $R \sqsubseteq P$ ).
  - ▶ from the functionality constraint on  $P$  and  $P(x_k, x_{k-1})$ , it can be inferred:  $y_k = x_{k-1}$ , and thus:  $R(x_k, x_{k-1})$
  - ▶ Now, based on the PI  $\exists R^- \sqsubseteq \exists R$ :  $\exists y_{k-1} R(x_{k-1}, y_{k-1})$ ,
  - ▶ and with the same reasoning as before, we get  $y_{k-1} = x_{k-2}$ , and thus:  $R(x_{k-1}, x_{k-2})$ .
  - ▶ By induction, it can be inferred:  $R(x_1, x)$ , and therefore  $r_k(x)$  is contained in the query  $q(x)$ .

## Problem with full DL-LITE by example - end

- One can show that for each  $k$ , there exists an Abox such that the reformulation  $r_k$  returns answers that are not returned by the reformulation  $r_{k'}$  for  $k' < k$ .
- Thus, there exists an infinite number of *non redundant* conjunctive reformulations.

# Outline

- 1 Introduction
- 2 3 ontology languages for the Web
- 3 Reasoning in Description Logics
- 4 Querying Data through Ontologies
- 5 Conclusion**

# Conclusion

- The scalability of reasoning on Web data requires **light-weight ontologies**
- One can use a description logic for which reasoning is feasible (polynomial)
- For ABoxes stored as relational databases, it is even preferable that query answering can be performed with a relational query (using query reformulation)
- Full OWL is too complex
- Consider extensions of RDFS